



## EXAM PAPERS PRACTICE

Boost your performance and confidence with these topic-based exam questions

Practice questions created by actual examiners and assessment experts

Detailed mark scheme

Suitable for all boards

Designed to test your ability and thoroughly prepare you

Mathematics: applications and interpretation Standard level

Level: IB Maths

Subject: IB Maths AI SL

Board: IB Maths

Topic: Past Paper 1

These Past Papers can be used by students and teachers and is  
Suitable for IB Maths AI SL Past Papers

# IB MATHS

# AI SL

## Key skills



## Instructions to Examiners

### Abbreviations

- M** Marks awarded for attempting to use a correct **Method**.
- A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- R** Marks awarded for clear **Reasoning**.
- AG** Answer given in the question and so no marks are awarded.

### Using the markscheme

#### 1 General

Award marks using the annotations as noted in the markscheme eg **M1**, **A2**.

#### 2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award **M0** followed by **A1**, as **A** mark(s) depend on the preceding **M** mark(s), if any.
- Where **M** and **A** marks are noted on the same line, e.g. **M1A1**, this usually means **M1** for an **attempt** to use an appropriate method (e.g. substitution into a formula) and **A1** for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies **M2**, **A3**, etc., do **not** split the marks, unless there is a note.
- Once a correct answer to a question or part-question is seen, ignore further correct working. However, if further working indicates a lack of mathematical understanding do not award the final **A1**. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal. However, if the incorrect decimal is carried through to a subsequent part, and correct **FT** working shown, award **FT** marks as appropriate but do not award the final **A1** in that part.

#### Examples

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	Award the final <b>A1</b> (ignore the further working)
2.	$\frac{1}{4}\sin 4x$	$\sin x$	Do not award the final <b>A1</b>
3.	$\log a - \log b$	$\log(a - b)$	Do not award the final <b>A1</b>



### 3 Implied marks

*Implied marks appear in **brackets e.g. (M1)**, and can only be awarded if **correct** work is seen or if implied in subsequent working.*

- Normally the correct work is seen or implied in the next line.
- Marks **without** brackets can only be awarded for work that is **seen**.

### 4 Follow through marks (only applied after an error is made)

*Follow through (**FT**) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) or subpart(s). Usually, to award **FT** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if the only marks awarded in a subpart are for the answer (i.e. there is no working expected), then **FT** marks should be awarded if appropriate.*

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** marks may be awarded if appropriate.
- If the question becomes much simpler because of an error then use discretion to award fewer **FT** marks.
- If the error leads to an inappropriate value (e.g. probability greater than 1, use of  $r > 1$  for the sum of an infinite GP,  $\sin \theta = 1.5$ , non integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word "their" in a description, to indicate that candidates may be using an incorrect value.
- Exceptions to this rule will be explicitly noted on the markscheme.
- If a candidate makes an error in one part, but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the question says hence. It is often possible to use a different approach in subsequent parts that does not depend on the answer to previous parts.

### 5 Mis-read

*If a candidate incorrectly copies information from the question, this is a mis-read (**MR**). Apply a **MR** penalty of 1 mark to that question*

- If the question becomes much simpler because of the **MR**, then use discretion to award fewer marks.
- If the **MR** leads to an inappropriate value (e.g. probability greater than 1,  $\sin \theta = 1.5$ , non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.
- The **MR** penalty can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.



## 6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, etc.
- Alternative solutions for part-questions are indicated by **EITHER . . . OR**.

## 7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation**.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, **simplified** answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).

## 8 Accuracy of Answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. There are two types of accuracy errors, and the final answer mark should not be awarded if these errors occur.

- **Rounding errors**: only applies to final answers not to intermediate steps.
- **Level of accuracy**: when this is not specified in the question the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.*

## 9 Calculators

A GDC is required for this examination, but calculators with symbolic manipulation features/ CAS functionality are not allowed.

### Calculator notation

The subject guide says:

*Students must always use correct mathematical notation, not calculator notation.*

Do **not** accept final answers written using calculator notation. However, do not penalize the use of calculator notation in the working.



1. (a) 210g A1  
[1 mark]
- (b) 240g A1  
[1 mark]
- (c)  $240 - 190$   
 $= 50\text{g}$  (M1)  
A1  
[2 marks]
- (d)  $240 + 1.5 \times (50)$   
 $= 315\text{g}$  M1  
A1  
[2 marks]

Total [6 marks]

2. (a)  $(d =) - 250$  A1  
[1 mark]
- (b)  $(u_{16} =) 6800 + (16 - 1)(- 250)$   
 $(\text{¥}) 3050$  M1  
A1  
[2 marks]
- (c)  $(S_{16} =) \left(\frac{16}{2}\right)(2 \times 6800 + (16 - 1)(- 250)) \times 2$  M1M1

**Note:** Award **M1** for correct substitution into arithmetic series formula.  
Award **M1** for multiplication by 2 seen.

OR

$$(S_{16} =) \left(\frac{16}{2}\right)(6800 + 3050) \times 2$$
M1M1

**Note:** Award **M1** for correct substitution into arithmetic series formula.  
Award **M1** for multiplication by 2 seen.

$$(\text{¥}) 158000 (157600)$$
A1  
[3 marks]

Total [6 marks]



3. (a) discrete

**A1**  
**[1 mark]**

(b) 
$$\frac{24 + 60 + 3k + 40 + 15 + 6}{88 + k} = 2$$

**M1A1**

**Note:** Award **M1** for substitution into the formula for the mean, award **A1** for a correct equation.

attempt to solve their equation

**(M1)**

$$k = 31$$

**A1**  
**[4 marks]**

(c) systematic



**A1**  
**[1 mark]**

**Total [6 marks]**



4. (a) 20

A1

[1 mark]

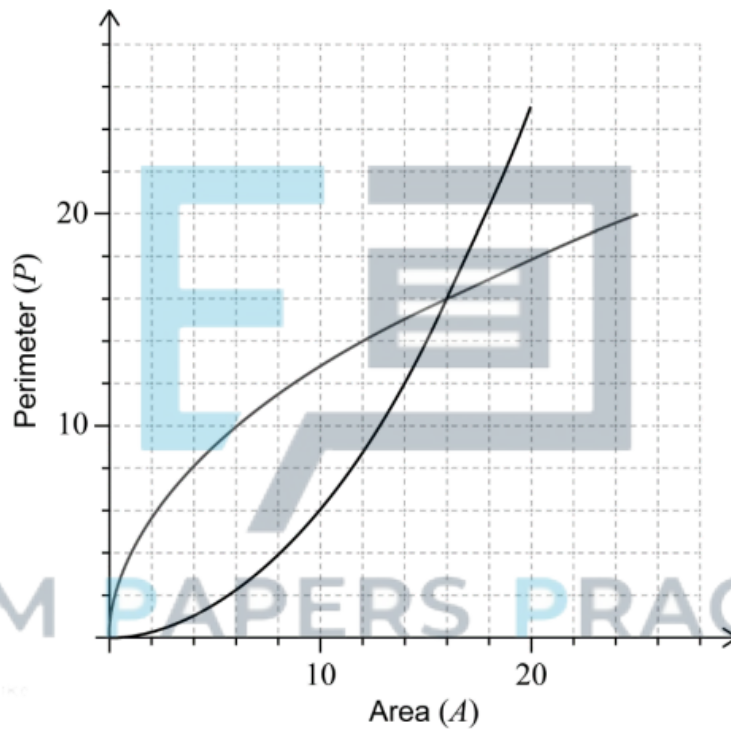
(b)  $n = 20$

A1

**Note:** Follow through from part (a).

[1 mark]

(c)



(M1)A1A1

(M1)A1A1

**Note:** Award (M1) for reflection in the line  $P = A$ , award A1 for endpoint at (20, 25), award A1 for passing through (16, 16).

[3 marks]

(d) when the perimeter is 8, the area is 4

A1

[1 mark]

Total [6 marks]



5. (a) (i) 1750 A1
- (ii)  $1350 + 400(1.25)^{-5}$  (M1)
- $= 1480$  A1

**Note:** Accept 1481.

[3 marks]

- (b)  $1400 = 1350 + 400(1.25)^{-t}$  (M1)
- 9.32 (days (9.31885...)) (days) A1

[2 marks]

- (c) 1350 A1

**Note:** Accept 1351 as a valid interpretation of the model as  $P = 1350$  is an asymptote.

[1 mark]

Total [6 marks]

6. (a) number of salad meals per week is independent of a person's position in the university A1

**Note:** Accept "not associated" instead of independent.

[1 mark]

- (b) 0.0201 (0.0201118...) A2

[2 marks]

- (c)  $0.0201 < 0.05$  R1
- the null hypothesis is rejected A1

[2 marks]

**Note:** Award (R1) for a correct comparison of their  $p$ -value to the test level, award (A1) for the correct interpretation from that comparison. Do not award (R0)(A1).

Total [5 marks]





7. (a)  $\frac{3-1}{7-3}$  (M1)  
= 0.5 A1  
[2 marks]

(b)  $y-2 = -2(x-5)$  (A1)(M1)

**Note:** Award (A1) for their  $-2$  seen, award (M1) for the correct substitution of (5, 2) and their normal gradient in equation of a line.

$2x + y - 12 = 0$  A1  
[3 marks]

- (c) every point in the cell is closer to E than any other snow shelter A1  
[1 mark]

Total [6 marks]

8. (a)  $10\log_{10}(6.4 \times 10^{-3} \times 10^{12})$  (M1)  
= 98.1(dB) (98.06179...) A1  
[2 marks]

- (b)  $112 = 10\log_{10}(S \times 10^{12})$  (M1)  
 $0.158(\text{W m}^{-2})(0.158489...(\text{W m}^{-2}))$  A1  
[2 marks]

Total [4 marks]



9. (a) (i)  $\mu_1 - \mu_2 = 0$  A1  
(ii)  $\mu_1 - \mu_2 \neq 0$  A1

**Note:** Accept equivalent statements in words.

[2 marks]

- (b) 0.296 (0.295739...) A2

[2 marks]

- (c)  $0.296 > 0.1$  R1

fail to reject the null hypothesis, there is no difference between the mean height of male and female students A1

**Note:** Award (R1) for a correct comparison of their  $p$ -value to the test level, award (A1) for the correct interpretation from that comparison. Do not award R0A1.

[2 marks]

Total [6 marks]

10. (a)  $A = \int_0^2 (6 - 3x)(4 + x) dx$  A1A1

**Note:** Award A1 for the limits  $x = 0$ ,  $x = 2$ . Award A1 for an integral of  $f(x)$ .

[2 marks]

- (b) 28 A1

[1 mark]

- (c)  $28 = 0.5 \times a \times 10$  M1

$$5.6 \left( \frac{28}{5} \right)$$
A1

[2 marks]

Total [5 marks]



$$11. \text{ volume} = 240 \left( \pi \times 8.4^2 - \frac{1}{2} \times 8.4^2 \times \frac{50 \times \pi}{180} \right)$$

**M1M1M1**

**Note:** Award **M1**  $240 \times \text{area}$ , award **M1** for correctly substituting area sector formula, award **M1** for subtraction of their area of the sector from area of circle.

$$= 45800 (= 45811.96071)$$

**A1**  
**Total [4 marks]**

$$12. (a) \frac{4}{18} \left( \frac{2}{9} \right)$$

**A1****[1 mark]**

$$(b) -3 \times \frac{1}{18} + (-1) \times \frac{4}{18} + 0 \times \frac{3}{18} + \dots + 5 \times \frac{7}{18}$$

**(M1)**

**Note:** Award **(M1)** for their correct substitution into the formula for expected value.

$$= 1.83 \left( \frac{33}{18}, 1.83333\dots \right)$$

**A1****[2 marks]**

$$(c) 2 \times \frac{1}{18} \times \frac{3}{18}$$

**(M1)(M1)**

**Note:** Award **(M1)** for  $\frac{1}{18} \times \frac{3}{18}$ , award **(M1)** for multiplying their product by 2.

$$= \frac{1}{54} \left( \frac{6}{324}, 0.0185185\dots, 1.85\% \right)$$

**A1****[3 marks]****Total [6 marks]**



13. (a)  $\frac{6}{15} \left( 0.4, \frac{2}{5} \right)$

A1

[1 mark]

(b)  $P(X = 8)$

(M1)

**Note:** Award (M1) for evidence of recognizing binomial probability.

eg,  $P(X = 8), X \sim B \left( 20, \frac{6}{15} \right)$ .

0.180 (0.179705...)

A1

[2 marks]

(c)  $P(\text{male}) = \frac{9}{15}$  (0.6)

A1

$P(X \leq 9) = 0.128$  (0.127521...)

(M1)A1

**Note:** Award (M1) for evidence of correct approach eg,  $P(X \leq 9)$ .

[3 marks]

Total [6 marks]



14. (a)  $\frac{\sin \hat{C}AB}{6} = \frac{\sin 15^\circ}{4.5}$  (M1)(A1)

$\hat{C}AB = 20.2^\circ$  (20.187415...) A1

**Note:** Award (M1) for substituted sine rule formula and award (A1) for correct substitutions.

[3 marks]

(b)  $\hat{C}BD = 20.2 + 15 = 35.2^\circ$  A1  
(let  $X$  be the point on  $BD$  where Ollie activates the sensor)

$\tan 35.18741\dots^\circ = \frac{1.8}{BX}$  (M1)

**Note:** Award A1 for their correct angle  $\hat{C}BD$ . Award M1 for correctly substituted trigonometric formula.

$BX = 2.55285\dots$  A1

$5 - 2.55285\dots$  (M1)

$= 2.45$  (m) (2.44714...) A1

[5 marks]

EXAM PAPERS PRACTICE Total [8 marks]